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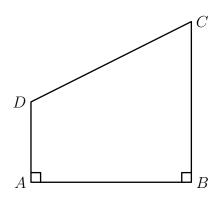
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Activity Sheet for the November, 2018, MATHCOUNTS Mini

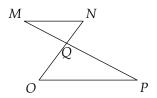


Try these problems before watching the lesson.

- 1. Point A is on segment \overline{BC} such that BA:AC=3:2. If BC=45, then what is the length of \overline{AC} ?
- 2. In trapezoid ABCD, AB = BC = 2AD and AD = 5 units. What is the area of trapezoid ABCD?



3. In the diagram below, $\overline{MN} \parallel \overline{OP}$, MN = 12, and OP = 20. If ON = 24, then what is QN?



4. Points A(0,0), B(6,0), C(6,10) and D(0,10) are vertices of rectangle ABCD, and E is on segment CD at (2,10). What is the ratio of the area of triangle ADE to the area of quadrilateral ABCE? Express your answer as a common fraction.

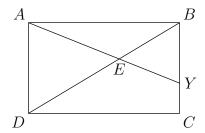




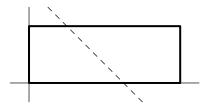
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First Problem: In rectangle ABCD, side AB has length 10 cm and side BC has length 6 cm. Point Y is on side BC such that CY = 2 cm. Segment AY intersects diagonal BD at point E. What is the length of segment AE?



Second Problem: The line x + y = 5 intersects a rectangle with vertices at (0,0), (0,3), (8,0) and (8,3), dividing it into two regions as shown. What is the ratio of the area of the smaller region to the area of the larger region?





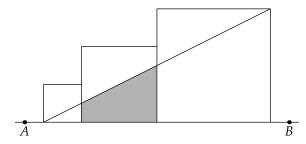


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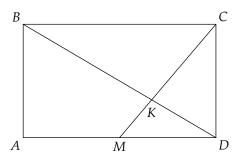


5. Three coplanar squares with sides of lengths two, four, and six units, respectively, are arranged side-by-side, as shown so that one side of each square lies on line AB and a segment connects the bottom left corner of the smallest square to the upper right corner of the largest square. What is the area of the shaded quadrilateral?



6. What is the area, in square units, of the interior region formed by the lines y = 2x - 4, y = -3x + 16 and the y-axis?

7. In rectangle ABCD, AB = 6 units, the measure of $\angle DBC$ is 30°, M is the midpoint of segment \overline{AD} and segments \overline{CM} and \overline{BD} intersect at point K. What is the length of segment \overline{MK} ?

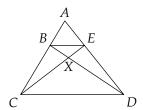






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8. In the diagram below, $\overline{BE} \parallel \overline{CD}$. If the area of trapezoid BCDE is 8 times the area of $\triangle ABE$, and the area of $\triangle CDX$ is 27 square units, then what is the area of $\triangle ACD$?





Have some thoughts about the video? Want to discuss the problems on the Activity Sheet? Visit the MATHCOUNTS Facebook page or the Art of Problem Solving Online Community (www.artofproblemsolving.com).