## 1 Art of Problem Solving

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Try these problems before watching the lesson.

1. In $\triangle X Y Z$, we have $\angle X=30^{\circ}, \angle Y=90^{\circ}$, and $Y Z=6$. Find $X Y$ and $X Z$.
2. What is the area of an equilateral triangle with side length 6 ?
3. What is the area, in square feet, of an isosceles triangle whose vertex angle is $120^{\circ}$ and whose base is 20 feet long? Express your answer as a common fraction in simplest radical form.
4. Billy is hiking in Colorado. He walks eastward four miles, then turns 60 degrees northward and walks six miles. How far is he from his starting point? Express your answer in simplest radical form.

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5^{2}
$$

First Problem: Congruent, non-overlapping circles $A, B, C$ and $D$ are positioned in a plane, such that $A, B$ and $C$ are mutually tangent to each other, and circle $D$ is tangent to circle $C$. Triangle $E F G$ circumscribes the four circles as shown. What is the length of side $F G$ ?


Second Problem: A unit square contains four congruent non-overlapping equilateral triangles as shown in the figure. What is the largest possible side-length of one of the triangles?

5. The altitudes of equilateral triangle $A B C$ all pass through point $H$ inside the triangle. If $A B=6$, then what is $A H$ ?
6. Six circles of radius 1 unit are drawn tangent to the sides of a regular hexagon. Each circle is also tangent to two other circles as shown in the drawing. What is the perimeter of the hexagon? Express your answer in simplest radical form.

7. Two angles of a triangle measure 30 and 45 degrees. If the side of the triangle opposite the 30 -degree angle measures $6 \sqrt{2}$ units, what is the sum of the lengths of the two remaining sides? Express your answer as a decimal to the nearest tenth.
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8. In triangle $A B C, m \angle A B C=120^{\circ}, A B=3$ and $B C=4$. If lines perpendicular to $\overline{A B}$ at point $A$ and to $\overline{B C}$ at point $C$ meet at point $D$, then find $C D$. (Source: AMC 12)


Have some thoughts about the video? Want to discuss the problems on the Activity Sheet? Visit the MATHCOUNTS Facebook page or the Art of Problem Solving Online Community (www.artofproblemsolving.com).

