

Activity Sheet for the January, 2020, MATHCOUNTS Mini



Try these problems before watching the lesson.

- 1. Kaylee cut a 20-cm by 20-cm piece of paper along a diagonal to form two congruent triangles. What is the length of the hypotenuse of one of the triangles? Express your answer in simplest radical form.
- 2. A triangular corner region is sliced off from a rectangular region as shown below. What is the area of the pentagonal region ABEFD that remains?



3. If altitude CD is $\sqrt{3}$ centimeters, what is the number of square centimeters in the area of ΔABC ?



4. Point A is on circle C and point P is outside the circle such that AP = 12 and \overline{AP} is tangent to the circle. If the circle has area 256π square units, then how far is P from the center of the circle?



The Problem

In the figure, square ABCD is divided into eight congruent right triangles and square EFGH, as shown. If the area of square ABCD is 1156 cm² and the area of square PQRS is 676 cm², what is the area of square EFGH?





- 5. Two circles with radii 16 and 9 are tangent to each other, and are tangent to line ℓ at distinct points P and Q. Find the length of \overline{PQ} .
- 6. In right triangle ABC, BD = CD + 9. If AB = 15 and BC = 39, what is AD?





- 7. Two angles of a triangle measure 45 and 105 degrees. If the side of the triangle opposite the 45-degree angle measures 8 units, what is the sum of the lengths of the two remaining sides?
- 8. In pentagon ABCDE, BC = CD = DE = 2 units, $\angle E$ is a right angle and $m \angle B = m \angle C = m \angle D = 135^{\circ}$. The length of segment AE can be expressed in simplest radical form as $a + 2\sqrt{b}$ units. What is the value of a + b?

Wow Share Your Thoughts

Have some thoughts about the video? Want to discuss the problems on the Activity Sheet? Visit the MATHCOUNTS Facebook page or the Art of Problem Solving Online Community (www.artofproblemsolving.com).